

# Eðlisfræði þéttfnis I

## Dæmablað 7

Skilafrestur 14. October 2014 kl. 15:00

### 1. Thermal conduction (10)

Explain why electrons carry a net energy but not a net current in the case of thermal conduction.

### 2. Dispersion relation (15)

Consider a linear chain in which alternate ions have mass  $M_1$  and  $M_2$ , and only nearest neighbors interact.

(a) Show that the dispersion relation for normal modes is

$$\omega^2 = \frac{K}{M_1 M_2} \left( M_1 + M_2 \pm \sqrt{M_1^2 + M_2^2 + 2M_1 M_2 \cos ka} \right)$$

(b) Discuss the form of the dispersion relation and the nature of the normal modes when  $M_1 \gg M_2$ . (i.e. calculate and draw the normal modes)

(c) Compare the dispersion relation with that of the monatomic linear chain when  $M_1 \sim M_2$ . (i.e. calculate and draw the normal modes)

### 3. Low-temperature specific heat in $d$ dimensions and for nonlinear dispersion (15)

Consider small lattice vibrations in a  $d$ -dimensional crystal in harmonic approximation.

- (a) For the Debye model, i.e. a linear dispersion  $\omega = c|k|$  of all phonon modes, calculate the phonon density of states and show that it varies as  $\omega^{d-1}$ . What is the Debye frequency ?
- (b) Determine the phonon contribution to low-temperature specific heat.
- (c) Investigate what would happen for a nonlinear phonon dispersion  $\omega \sim |k|^\nu$  (anomalous sound). Show that the low-temperature specific heat would vanish as  $T^{d/\nu}$  in  $d$  dimensions.