On low pressure electronegative capacitive discharges

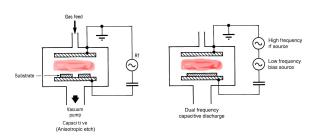
Jón Tómas Guðmundsson^{1,2}

¹Space and Plasma Physics, KTH Royal Institute of Technology, Stockholm, Sweden ²Science Institute, University of Iceland, Reykjavik, Iceland tumi@hi.is

6th DUT-RUB-WIGNER Workshop on Low Temperature Plasma Science Dalian, China September 17., 2025



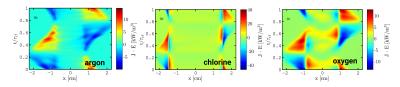




Lieberman and Lichtenberg (2025), Principles of Plasma Discharges and Materials Processing, 3rd edition, Wiley

- The capacitive discharge is sustained by applying radio-frequency (rf) voltage or current between electrodes when a neutral gas at low pressure is injected
- The discharge is sustained by radio-frequency (rf) currents and voltages, introduced through capacitive sheaths



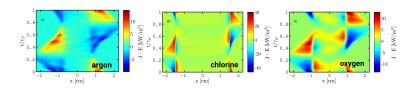


- The two main electron power absorption mechanisms in these discharges are
 - momentum transfer due to the moving sheaths which leads to stochastic (pressure or collisionless) heating
 - currents in the main body of the plasma discharge lead to Ohmic (or collisional) heating in the bulk and sheath regions
- We explore this using 1D particle-in-cell/Monte Carlo collision simulation for three different chemistries
 - weakly electronegative oxygen discharge
 - highly electronegative chlorine discharge
 - electropositive argon discharge

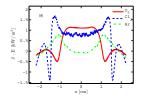








- The electron power absorption
 - p = 1.33 Pa
 - *f* = 13.56 MHz
 - $V_0 = 222 \text{ V}$
 - gap = 45 mm
- lacktriangle For argon the discharge is in lpha-mode
- Chlorine and oxygen discharges operate in hybrid α and drift ambipolar (DA)-mode







Outline

- The 1D particle-in-cell/Monte Carlo collision simulation
- The low pressure oxygen discharge
- The low pressure chlorine discharge
- The argon discharge
- Argon discharge diluted by chlorine
- Summary





The 1D particle-in-cell/Monte Carlo collision simulation





The oopd1 1d-3v PIC/MCC code

- We use the oopd1 (objective oriented plasma device for one dimension) code to simulate the discharges
- The oopd1 code was originally developed by the Plasma Theory and Simulation Group at UC Berkeley later Michigan State University
- It has 1 dimension in space and 3 velocity components for particles (1d-3v)
- The oopd1 code is supposed to replace the widely used xpdx1 series (xpdp1, xpdc1 and xpds1)
- It is developed to simulate various types of plasmas, including processing discharges, accelerators and beams
 - Modular structure
 - Includes relativistic kinematics
 - Particles can have different weights



The low pressure oxygen discharge





- Oxygen forms a weakly electronegative discharge
- The oxygen discharge is of vital importance in various materials processing applications such as
 - ashing of photoresist
 - etching of polymer films
 - oxidation and deposition of thin film oxides
- The presence of negative ions has a strong influence on the kinetics and dynamics of the oxygen discharge
- The oxygen chemistry is rather involved, in particular due to the presence of **metastable molecular and atomic** oxygen and their role in dissociative attachment and detachment processes





The oxygen discharge

- We consider a discharge that consists of:
 - electrons
 - the ground state oxygen molecule $O_2(X^3\Sigma_a^-)$
 - the metastable oxygen molecule $O_2(a^1\Delta_a)$
 - the metastable oxygen molecule $O_2(b^1\Sigma_a)$
 - the ground state oxygen atom O(³P)
 - the metastable oxygen atom O(¹D)
 - the negative oxygen ion O⁻
 - the positive oxygen ions O⁺ and O₂⁺

Gudmundsson and Lieberman (2015) Plasma Sources Sci. Technol., 24 035016

Hannesdottir and Gudmundsson (2016) Plasma Sources Sci. Technol., 25 055002

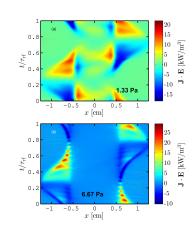
Gudmundsson and Proto (2019) Plasma Sources Sci. Technol.. 28 045012

We apply a global model beforehand to calculate the partial pressure of the various neutrals



Oxygen CCP - pressure dependence

- A parallel plate capacitively coupled oxygen discharge at driving frequency of 13.56 MHz for gap separation of 45 mm
- The spatio-temporal electron heating J_e · E at 1.33 Pa (upper graph) and 6.67 Pa (lower graph)
- At 1.33 Pa there is a significant electron power absorption within the electronegative core
- At 6.67 Pa the electron power absorption occurs almost solely in the sheath region



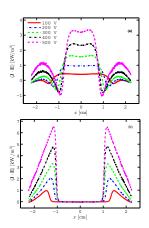






Oxygen CCP - pressure dependence

- The time averaged electron power absorption ⟨J_e · E⟩ at 1.33 Pa (upper graph) and 6.67 Pa (lower graph)
- At 1.33 Pa there is significant electron power absorption within the electronegative core
- At 6.67 Pa, the electron power absorption the electronegative core is roughly zero, and the electron power absorption is almost entirely located in the sheath regions

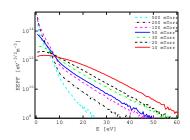






Oxygen CCP – pressure dependence

- At low pressure (< 4 Pa) the EEPF is Druyvesteyn like and becomes bi-Maxwellian as the pressure is increased
- These results contradict what is commonly found for the capacitively coupled argon discharge where the EEPF evolves from being bi-Maxwellian at low pressure to being Druyvesteyn like at high pressure



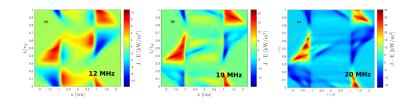
Gudmundsson and Ventéjou (2015) JAP 118 153302







Oxygen CCP – frequency dependence



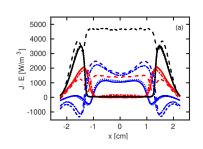
Gudmundsson et al. (2018), PSST 27(2) 025009

- Oxygen discharge at 1.33 Pa
- At 12 MHz significant power absoption is observed in the plasma bulk but also in the sheath region
- At 19 MHz the heating and cooling in the sheath regions has increased, however there is contribution to the electron power absorption in the bulk region (note the change in scale)
- At 20 MHz there is almost no electron power absorption in the plasma bulk

Oxygen CCP - pressure dependence

- At 1.33 Pa excluding the metastable states in the simulation has very small influence on the heating mechanism
- At 6.67 Pa the metastable states have a significant influence on the heating mechanism and even more significant at 26.67 Pa
- This is due to detachment by the metastable $O_2(a^1\Delta_q)$ molecule

$$O^- + O_2(a^1 \Delta_g) \rightarrow products$$



Gudmundsson and Ventéjou (2015) JAP 118 153302

Gudmundsson and Lieberman (2015) PSST 24 035016

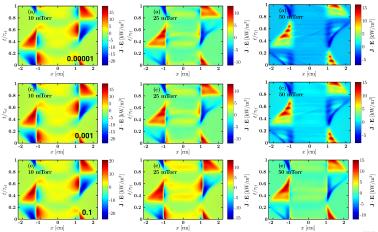
Gudmundsson and Hannesdottir, AIP

Conf. Proc. (2017) 1811 120001





Oxygen CCP – surface quenching of $O_2(a^1\Delta_g)$

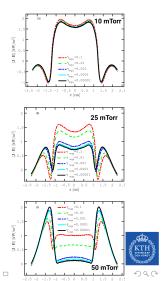


Oxygen CCP – surface quenching of $O_2(a^1\Delta_g)$

- At 1.33 Pa (10 mTorr) almost all the electron heating occurs in the plasma bulk (the electronegative core) and the electron heating profile is independent of the surface quenching coefficient
- At 6.67 Pa (50 mTorr) only for the highest surface quenching coefficients 0.1 and 0.01 there is some electron heating observed in the bulk region
- Typical value is 0.007 for iron

Sharpless and Slanger (1989) Journal of Chemical Physics 91 7947

Proto and Gudmundsson (2018) PSST 27 074002 (2018)



Electron power absorption - Bolzmann term analysis

■ To determine the electron power absorption mechanisms we apply Boltzman term analysis

Surendra and Dalvie (1993) PRE 48(5) 3914 and Schulze et al. (2018) PSST 27(5) 055010

- The electric field within the electronegative core constitutes contributions through various different phenomena
- The electric field is composed of six terms

$$E = -\underbrace{\frac{m_{e}}{e} \frac{\partial u_{e}}{\partial t}}_{I} + \underbrace{\frac{m_{e}}{e} \frac{u_{e}^{2}}{n_{e}} \frac{\partial n_{e}}{\partial x}}_{II} + \underbrace{\frac{m_{e}}{e} \frac{u_{e}}{n_{e}} \frac{\partial n_{e}}{\partial t}}_{III} - \underbrace{\frac{T_{e}}{n_{e}} \frac{\partial n_{e}}{\partial x}}_{IV} - \underbrace{\frac{\partial T_{e}}{\partial x}}_{V} - \underbrace{\frac{m_{e}u_{e}v_{c}}{e}}_{VI}$$





Electron power absorption - Bolzmann term analysis

The electron absorbed power can be determined as follows

$$J_{e} \cdot E = \underbrace{m_{e} u_{e} n_{e} \frac{\partial u_{e}}{\partial t}}_{I} - \underbrace{m_{e} u_{e}^{3} \frac{\partial n_{e}}{\partial x}}_{II} - \underbrace{m_{e} u_{e}^{2} \frac{\partial n_{e}}{\partial t}}_{III}$$
$$+ \underbrace{e u_{e} T_{e} \frac{\partial n_{e}}{\partial x}}_{IV} + \underbrace{e n_{e} u_{e} \frac{\partial T_{e}}{\partial x}}_{V} + \underbrace{m_{e} n_{e} \nu_{c} u_{e}^{2}}_{VI}$$
(1)

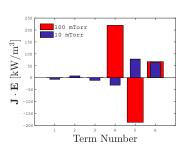
- Terms I and III power absorption due to electron inertia
- Term II the electron density gradient
- Term IV ambipolar field electron density gradient
- Term V the electron temperature gradient
 - Terms IV and V are pressure or collisionless heating
- Term VI electron neutral collisions or Ohmic heating





Oxygen CCP - Bolzmann term analysis

- The pressure terms are important significant part of the electron power absorption at both 1.33 Pa and 13.3 Pa is due to the pressure terms
- The Terms IV (ambipolar) and V (electron temperature gradient) flip signs and are sharply smaller in the absolute value at 1.33 Pa
- The Ohmic term's magnitude (Term VI) is similar at both pressures
- Note that Ohmic power absorption is important even at low pressure



Proto and Gudmundsson (2020) JAP 128 113302







The low pressure chlorine discharge





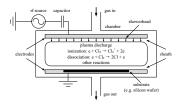
The chlorine discharge

- Chlorine is an electronegative diatomic gas that is widely used in plasma etching of both semiconductors and metals, in particular poly-silicon gate and aluminum interconnects
- Chlorine atoms are believed to be the primary reactant in plasma etching
- The chlorine molecule has
 - a low dissociation energy (2.5 eV)
 - a near-zero threshold energy for dissociative attachment
- All electronic excitations of the molecule appear to be dissociative, and no metastable molecular states are of importance





The chlorine discharge

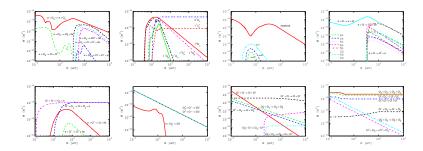


- We consider a discharge that consists of:
 - electrons
 - the ground state chlorine molecule $\operatorname{Cl}_2(X^1\Sigma_g^+, v = 0)$,
 - the ground state chlorine atom Cl(3p⁵ ²P)
 - the negative chlorine ion CI[−]
 - the positive chlorine ions Cl⁺ and Cl₂⁺
- We apply a global model beforehand to calculate the fraction of CI atoms



900

The chlorine discharge



■ The reaction set for the chlorine is comprehensive and includes 44 reactions

Huang and Gudmundsson (2013) Plasma Sources Sci. Technol., 22(5) 055020





Voltage source operated at a single frequency

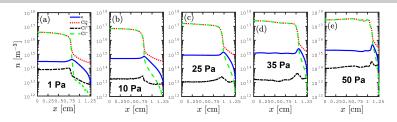
$$V(t) = V_{\rm rf} \sin(2\pi f t)$$

gap = 2.54 cm, V_{rf} = 222 V and f = 13.56 MHz





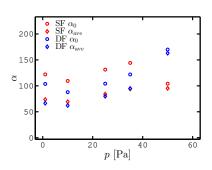




Proto and Gudmundsson (2021) PSST 30(6) 065009

- The time averaged charged particle density profiles of a parallel plate capacitively coupled chlorine discharge
- At low pressures, the profile for Cl₂⁺ ions is cosine-like or parabolic since Cl₂⁺ ions are lost mainly due to diffusion to the walls
- As the pressure increases, the recombination between Cl₂⁺ and Cl⁻ ions becomes the major loss mechanism for Cl₂⁺ ions and the density profile for Cl₂⁺ and Cl⁻-ions becomes flat in the bulk region

- The electronegativity in the discharge center is very high and increases with increased operating pressure
- Negative ion creation proceeds via electron impact dissociative attachment whose cross-sections are high
- Drift-ambipolar (DA) power absorption is expected within the electronegative core



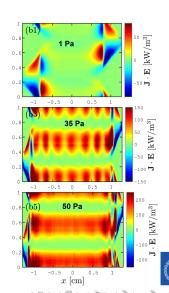
Skarphedinsson and Gudmundsson (2020) PSST 29(8) 084004

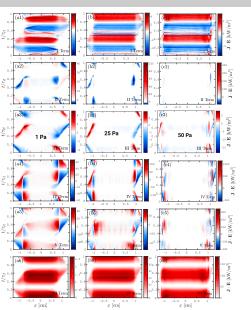






- The spatio temporal behavior of the total electron power absorption
 J_e · E over the full gap length for a capacitively coupled chlorine discharge
- At 1 Pa there is clear sign of drift ambipolar heating (DA-mode) and stochastic heating (α-mode)
- At 35 and 50 Pa there are indications of striations in addition to drift ambipolar heating (DA-mode) and stochastic heating (α-mode)





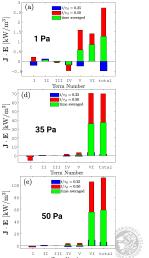
- The spatio temporal behavior of the various terms that constitute the electron power absorption
 - Terms I and III electron inertia
 - Term I electron density gradient
 - Terms IV and V pressure (collisionless) heating
 - Term VI Ohmic heating

Proto and Gudmundsson (2021) PSST 30(6) 1665



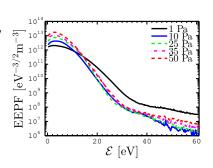
- The space averaged electron power absorption profile terms
 - \bullet $t/\tau_{\rm rf} = 0.25$ blue bar
 - $t/\tau_{\rm rf} = 0.5 \text{ red bar}$
 - time averaged green bar
- At 1 Pa the pressure terms and the Ohmic term contribute to the electron power absorption
- At higher pressures Ohmic power absorption dominates

Proto and Gudmundsson (2021) PSST 30(6) 065009





- The electron energy probability function (EEPF) in the discharge center is Druyvesteyn like at all pressures
- This is expected when there is significant Ohmic heating in the plasma bulk







Striations

Voltage source operated at a single frequency

$$V(t) = V_{\rm rf} \sin(2\pi f t)$$

gap = 2.54 cm, V_{rf} = 222 V and f = 13.56 MHz

$$\gamma_{\rm i}(\mathcal{E}_{\rm i}) + \gamma_{\rm n}(\mathcal{E}_{\rm n}) + \gamma_{\rm e}(\mathcal{E}_{\rm e}, \theta)$$

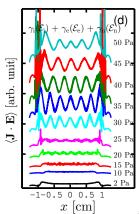






Striations

- Primary electron power absorption as the pressure is varied
- We observe striation pattern at 15Pa
- Above 15 Pa the striation amplitude increases with increased pressure up to 35 Pa, and then decreases
- The number of striations decreases with increased pressure







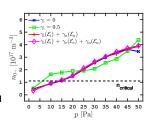
Mahdavipour and Gudmundsson (2025) PSST 34(4) 045005

Striations

- Striations are known to appear in electronegative discharges when two conditions are simultaneously fulfilled:
 - high enough electronegativity
 - driving frequency that is comparable to the ion plasma frequency
- Based on the ion-ion plasma model striations may appear when $n_{\text{ion}} > n_{\text{critical}}$ where the critical density is defined as

$$n_{\text{critical}} = \frac{\omega_{\text{rf}}^2 \epsilon_0 \mu}{e^2}$$

where $\mu = m_+ m_- / (m_+ + m_-)$ is the reduced mass of the positive and negative ions



Mahdavipour and Gudmundsson (2025)

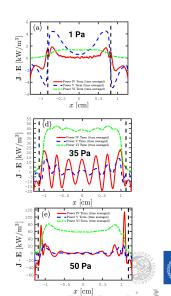
PSST **34**(4) 045005





Striations - electron power absorption

- The time averaged electron power absorption profile of
 - term IV (red line)
 - term V (blue dashed line)
 - term VI (green dot dashed line)
- At 1 Pa the pressure terms and the Ohmic term contribute to the electron power absorption
- At higher pressures Ohmic power absorption dominates
- At 35 Pa striations are observed the pressure terms are apparent



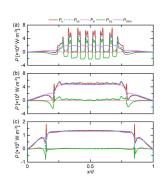
Striations – electron power absorption

- Similar findings have been reported more recently for a capacitive CF₄ discharge operated at 60 Pa and 6.78 MHz with 2 cm electrode gap (top graph)
- In this case the pressure terms

$$P_{\nabla p} = \underbrace{eu_{e}T_{e}\frac{\partial n_{e}}{\partial x}}_{\text{IV}} + \underbrace{en_{e}u_{e}\frac{\partial T_{e}}{\partial x}}_{\text{V}}$$

dominate the power absorption process

 For higher operating frequency the Ohmic term dominates the electron power absorption (lower graphs)



Zhou et al. (2025) PSST 34(8) 085014







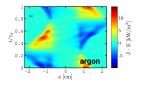
The argon discharge

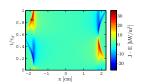




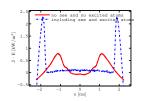


Introduction





- The electron power absorption
 - p = 1.33 Pa
 - *f* = 13.56 MHz
 - $V_0 = 222 \text{ V}$
 - gap = 45 mm
 - lacktriangle no excited argon states and $\gamma_{
 m see}=$ 0.0 (left)
 - with excited argon states and $\gamma_i(\mathcal{E}_i) + \gamma_n(\mathcal{E}_n) + \gamma_e(\mathcal{E}_e, \theta)$ (right)
- For argon the discharge is in α -mode



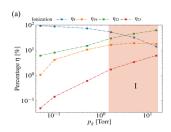






The argon discharge

- The ionization processes versus pressure neglecting secondary electrons
 - Electron impact ionization
 - Step-wise ionization
 - Metastables pooling ionization
 - Metastables pooling ionization
- The region labeled I (pg > 200 Pa) indicates where the contributions of metastable pooling and step-wise ionization exceed that of electron impact ground state ionization







Current source operated at a single frequency

$$J(t) = J_{\rm rf} \sin(2\pi f t)$$

gap = 2.54 cm, J_{rf} = 50 A/m² and f = 13.56 MHz, p = 6.67 Pa







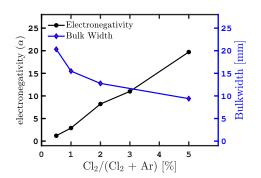
Case	exited species	ions	neutrals	electrons
 	0.0 included included	$0.0 \\ 0.0 \\ \gamma_{\mathrm{see,i}}(\mathcal{E}_{\mathrm{i}})$	$0.0 \ 0.0 \ \gamma_{ m see,n}(\mathcal{E}_{ m n})$	$0.0 \ 0.0 \ \gamma_{ m see,e}(\mathcal{E}_{ m e}, heta)$

We explored three cases

- Neglecting excited states of argon and all secondary electron emission
- Including excited states of argon and neglecting all secondary electron emission
- Including excited states of argon and all secondary electron emission



- Ar/Cl₂ mixture at 6.67 Pa
- The electronegativity increases with increased chlorine fraction
- The plasma bulk width decreases with increased chlorine fraction
- Gap width 2.5 cm, driving current density 50 A/m² and frequency 13.56 MHz
- The argon model includes excited argon atoms

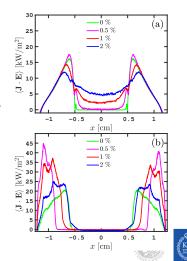




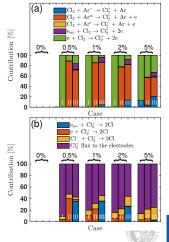




- Ar/Cl₂ mixture at 6.67 Pa
- The time-averaged electron power absorption for varying chlorine dilution
 - (a) neglecting excited argon states
 - (b) including excited argon states



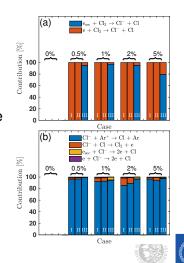
- Ar/Cl₂ mixture at 6.67 Pa
- The creation and loss of the Cl₂⁺ ion
- The role of Penning ionization becomes rather significant as excited states of argon are included in the discharge model
- Gap width 2.5 cm, driving current density 50 A/m² and frequency 13.56 MHz





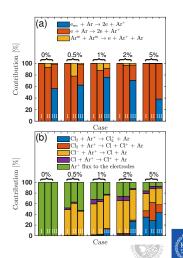


- Ar/Cl₂ mixture at 6.67 Pa
- The creation and loss of the negative CI⁻ ion
- The creation of the negative ion Cl[−] is almost entirely due to dissociative attachment as for pure chlorine discharge
- The role of secondary electrons becomes significant as they are included in the discharge model
- Ion-ion recombination with Ar⁺ is the main loss process





- Ar/Cl₂ mixture at 6.67 Pa
- The creation and loss of the Ar⁺ ion
- The contribution of secondary electrons becomes significant as they are included in the discharge model

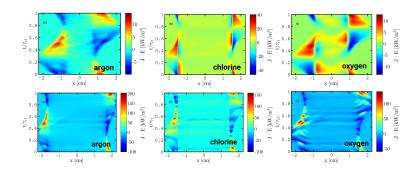


Summary





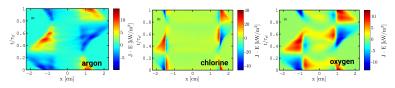
Summary



 Capcacitively coupled argon, oxygen and chlorine discharges were studied by particle-in-cell/Monte Carlo collision simulations



Summary



- In a chlorine discharge DA electron power absorption dominates and becomes increasingly more Ohmic with increased pressure
- Including the detachment processes by the singlet metastable states has a strong influence on the electronegativity in the oxygen discharge
- A heating mode transition, from hybrid drift-ambipolar (DA) and α -mode to pure α -mode, is observed as the pressure, driving frequency, or electrode gap spacing are increased, or the quenching coefficient of the oxygen metastable $O_2(a^1\Delta_a)$ is varied



Acknowledgements

Thank you for your attention

The slides can be downloaded at

http://langmuir.raunvis.hi.is/~tumi/ranns.html

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