

# The Low Pressure Inductive Discharge

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## Partially ionized plasma

- A plasma is a collection of free charged particles, electrically neutral on the average
- The plasma is either partially or fully ionized gas that contains electrons, ions, neutral atoms and molecules
- In partially ionized plasma discharges charged particles usually interact weakly with each other and electron collisions are most frequent with neutral atoms and molecules
- Ionization of neutrals sustains the plasma in the steady state
- The electrons are not in thermal equilibrium with the ions

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## Overview

- Partially ionized plasma
- Discharges
- Inductive Discharges
- Planar Inductive Discharge
- Electromagnetic modeling
- Global model of plasma chemistry

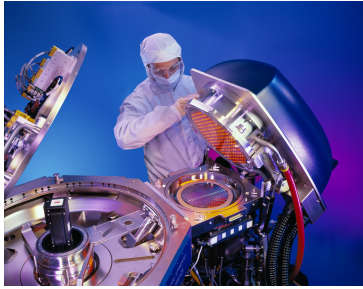
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## Partially ionized plasma

- A plasma is characterized by the plasma parameters, particle equilibrium temperatures and particle densities
- Each species can have its own thermal equilibrium temperature
- Here we will limit the discussion to low pressure discharges
- Low pressure discharges are characterized by
  - $T_e \approx 1 - 10 \text{ eV}$
  - $T_i \ll T_e$
  - $n_e \approx 10^{14} - 10^{19} \text{ m}^{-3}$
- The neutral gas pressure is low
  - $p \approx 1 \text{ mTorr} - 1 \text{ Torr}$ .

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## Partially ionized plasma



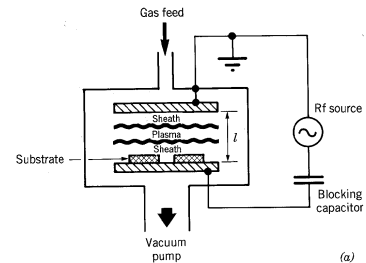
- Low pressure, weakly ionized, non-equilibrium gas discharge plasmas are used for a variety of materials processing applications
- The primary use of plasma processing in the electronics industry is in semiconductor chip manufacturing
- In integrated circuit processing plasma processes are essential in achieving the small feature sizes and packing density required by the electronics industry

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## Discharges

### Capacitive discharge

- In the early days capacitively driven radio frequency (rf) discharges were commonly used for dry etching



- A conventional capacitively coupled, rf, parallel plate electrode discharge
- Batches of wafers are loaded onto one of the electrodes, either powered or grounded

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## Partially ionized plasma



- New high density plasma sources are being developed to meet the requirements for the future integrated circuit devices
- The simplest and most convenient design for a high density discharge for materials processing is the planar inductive discharge which evolved from a century old idea

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## Discharges

### Capacitive discharge

- The typical rf driving voltage is  $V_{rf} \approx 100 - 1000 \text{ V}$  operated at 13.56 MHz driving frequency and the electrode separation is  $l \approx 2 - 10 \text{ cm}$
- Typical gas pressures are in the range 10 – 100 mTorr, and plasma densities are relatively low, typically  $10^{15} - 10^{17} \text{ m}^{-3}$
- Ion acceleration energy  

$$\sim V_{rf}/2$$
- The plasma density is controlled by the applied rf voltage which also determined the ion energy
- No independent control of plasma parameters, such as electron and ion energy, charge density, and reactant density
- The capacitive discharge dominated in the industry until 1994

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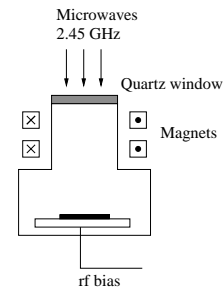
## Discharges

- In the early 1990's plasma processing changed from batch operations to single-wafer operations with 150 mm diameter wafers; wafer sizes are now 300 mm diameter
- For single wafer processing and submicron dry etching, a high plasma density and low neutral gas pressure are desired to obtain the desired profiles and processing rates to compensate for the inherent throughput problem of a single-wafer processing
- This has led to the development of a new generation of low pressure, high-density plasma sources, where the rf or microwave power is coupled to the plasma via a dielectric window

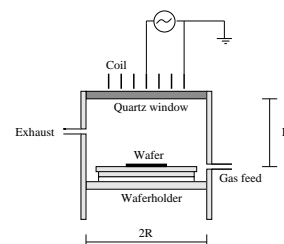
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## Discharges

### Electron cyclotron resonance (ECR) discharge



### Planar inductively coupled discharge



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## Discharges - Challenges

- High density
  - Higher etch and deposition rates
- Low pressure
  - Reduce scattering (anisotropy)
- Uniformity
  - Larger wafers
- Low and controllable ion energy
  - Radiation damage

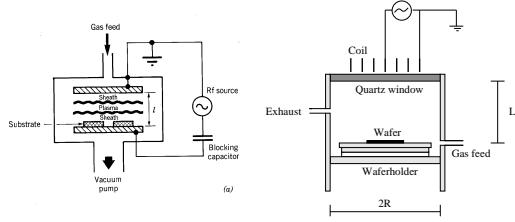
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## Discharges

- The inductive and ECR discharges give 1 – 2 orders of magnitude ion density than a capacitively coupled discharge
- Ion bombarding energy is about an order of magnitude lower (and is controllable)
- In these new discharges there is independent control of ion density and ion bombarding energy
  - The ion density is controlled by the power applied to the inductive coil (or microwave power)
  - The ion energy can be controlled by rf bias applied to the substrate holder
- Currently the inductive discharge dominates in the electronics industry

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## Discharges



	Capacitive discharge	High density
Gas pressure [mTorr]	10 – 1000	0.5 – 50
Power [W]	50 – 2000	100 – 5000
Driving frequency [Mhz]	0.05 – 13.56	0 – 2450
Electron density [ $\text{cm}^{-3}$ ]	$10^9 - 10^{10}$	$10^{10} - 10^{12}$
Electron temperature [eV]	1 – 5	2 – 7
Ion energy [V]	200 – 1000	< 100

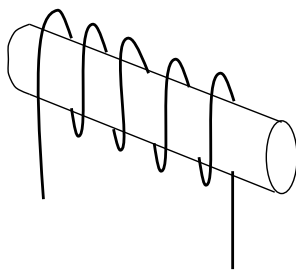
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## The inductive discharge

- These early experiments caught the interest of J. J. Thomson who repeated the experiments [Thomson, 1891].
- Consequently Thomson developed a theory assuming a purely inductive coupling mechanism
- The discharge was taken to be a single turn lossy conductor that is coupled to the non-resonant coil
- The discharge forms a secondary loop that has resistance  $R_2$ , a self inductance  $L_2$  and a mutual inductance with the primary circuit  $M$

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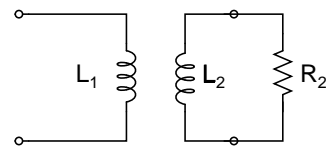
## The inductive discharge



- An inductive discharge in its simplest form is a tube made of quartz or ceramic placed inside a solenoid (the primary coil) through which rf current is applied
- The inductive discharge was introduced by W. Hittorf in 1884 [Hittorf, 1884]
- He describes a method to send a current, induced by another current, through a gas, without electrodes

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## The inductive discharge



- The resistance change seen in the primary loop due to the discharge loop is then

$$\rho' = \frac{\omega^2 M^2 R_2}{R_2^2 + \omega^2 L_2^2}$$

where  $\omega$  is the driving frequency of the current in the primary circuit

- N. Tesla was convinced that the discharge was primarily of electrostatic nature, a result of the large potential difference which exists between the ends of the inductive coil [Tesla, 1891]
- The nature of the discharge was a debate for over five decades and is still not fully resolved

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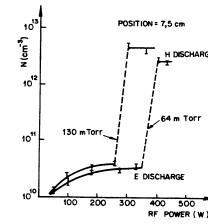


## The inductive discharge

- MacKinnon [MacKinnon, 1929] resolved this question by demonstrating that as the power is increased, a weak capacitively coupled electrostatic mode (E-mode) precedes the inductively coupled magnetic mode (H-mode).
- The discharge is either maintained by the axial electrostatic field or by an azimuthal electromagnetic field of the inductor coil
- To reach the magnetic mode the applied power and current has to exceed a critical limit
- The electrostatic mode is characterized by a uniform faint glow
- The electromagnetic mode is characterized by a bright ring-like discharge due to the limited skin depth of the exciting field (the periphery glows more brightly)

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## The inductive discharge

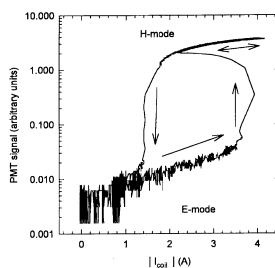


[Amorim et al., 1991]

- The change from electromagnetic mode to electrostatic mode is generally at lower power than the change from electrostatic to electromagnetic mode
- The change in brightness is attributed to the abrupt change in electron density that occurs when the discharge goes through the transition
- This change in density can be from a low density mode  $n_e < 10^{17} \text{ m}^{-3}$  to a high density mode  $n_e > 10^{17} \text{ m}^{-3}$

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## The inductive discharge

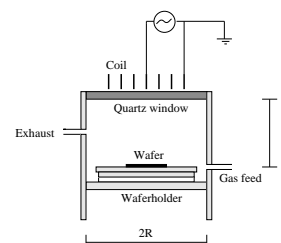


[Kortshagen et al., 1996]

- When the discharge changes from the electrostatic mode to the electromagnetic mode the brightness increases abruptly
- This change in light intensity can be a few orders of magnitude
- Decreasing the applied power dims the discharge emission slightly until an abrupt change to much lower emission occurs

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## The planar inductive discharge



- Around the mid-to-late 1980's inductive systems were introduced to plasma processing
- Their simple design, construction and operation make them attractive for industrial applications such as in etching and deposition processes

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## The planar inductive discharge

- Other advantages include no need for dc magnetic fields and the use of an rf power source rather than a microwave source
- For materials processing they are often operated in low pressure ( $< 50$  mTorr) and in low aspect ratio geometries,  $L/R \leq 1$  for a cylindrical discharge, and can be driven by a planar coil
- The inductive coils are most commonly driven at 13.56 MHz or below, using a  $50\ \Omega$  rf power supply through a capacitive matching network
- An electrostatic shield is often placed between the coil and the plasma to reduce possible capacitive coupling

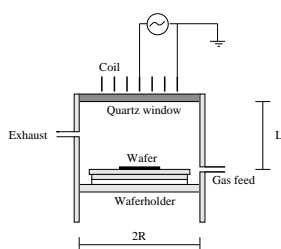
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## The planar inductive discharge

- The inductive power transfer and lack of electrodes leads to low voltages across all plasma sheaths and wall surfaces
- The dc plasma potential and hence the ion acceleration energy is typically 20 – 40 V at all surfaces
- To control the ion energy the substrate is placed on an electrode that can be independently driven by a capacitively coupled rf source
- Thus there is an independent control of the ion/radical fluxes (through the inductive source power) and the ion-bombarding energy (through the substrate electrode)

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## The planar inductive discharge



- The substrate may be placed in close proximity to the inductive coil
- In the planar configuration the coil is typically separated from the plasma by a 1 – 3 cm thick quartz window and the substrate is placed 5 – 10 cm below the window (3 - 10 skin depths)

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## Electromagnetic modeling - Power transfer

Primary goal:

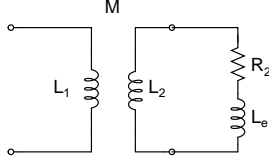
- Relate the plasma parameters (electron density and temperature) to the external electrical characteristics of the discharge such as the rf current and rf voltage

Method:

- Apply Thomson's transformer model of the inductive discharge
- Develop a first principles model of the components of the transformer circuit
- Use a global model of the plasma chemistry to estimate the plasma parameters

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## Electromagnetic modeling - Power transfer



- $L_2$  is the geometric inductance of the plasma
- $L_e$  is the inertia inductance
- $R_2$  is the plasma resistance
- $M$  is the mutual inductance between the primary and secondary circuit

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## Electromagnetic modeling

- For a planar inductively coupled discharge the magnetic induction components  $B_r(r, z)$  and  $B_z(r, z)$ , the electric field component  $E_\theta(r, z)$  and the plasma current are calculated assuming axisymmetric geometry
- The mutual inductance between the primary and secondary circuit  $M$ , the self inductance of the plasma  $L_2$  and the impedance of the plasma are determined theoretically and related to the properties of the plasma
- The planar inductive discharge is modeled as a transformer with the inductive coil taken as the primary circuit and the plasma as the secondary circuit to find the impedance characteristics in the primary circuit due to plasma load.

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## Electromagnetic modeling

- Seen in the primary circuit the effect of the coupled secondary circuit is to add the impedance

$$Z_2(\omega M)^2 / |Z_2|^2$$

to the primary circuit, where

$$Z_2 = R_2 + j\omega [L_2 + L_e]$$

is the complex impedance of the secondary circuit

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## Electromagnetic modeling

- Plasma resistance

$$R_2 \sim f(\nu_{\text{eff}}, n_e, \text{electric field profile})$$

- Effective collision frequency

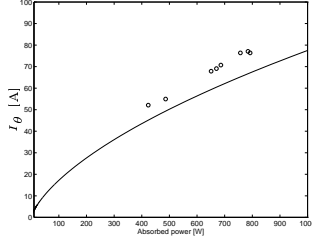
$$\nu_{\text{eff}} = \nu_{\text{en}} + \nu_{\text{st}} + \nu_{\text{ei}}$$

- Electron density and temperature are related to pressure and applied power via the global (volume averaged) model
- Electron inertia inductance

$$L_e = R_2 \frac{\omega_{\text{eff}}}{\omega} \nu_{\text{eff}}$$

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## Electromagnetic modeling



- The induced plasma current  $I_\theta$  versus the absorbed power for argon plasma at 120 mTorr neutral gas pressure, driving frequency  $f = 0.56$  MHz and dimensions  $R = 16$  cm and  $L = 20$  cm

$$I_\theta = (P_{\text{abs}}/R_2)^{1/2}$$

$$E_\theta = E_{\theta 0} J_1(\gamma_1 r) \exp(-z\gamma)$$

- The solid line shows the model estimate and the circles the measured data (from [El-Fayoumi, 1996])

## Electromagnetic modeling

- The magnetic induction along the axis

$$B_{zi}(r, z) = \frac{\mu_0 I_r f}{2\pi} \frac{1}{((a_i + r)^2 + z^2)^{1/2}} \times \left[ K(\kappa_i) + \frac{a_i^2 - r^2 - z^2}{(a_i - r)^2 + z^2} E(\kappa_i) \right]$$

and in the radial direction

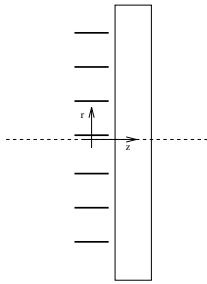
$$B_{ri}(r, z) = \frac{\mu_0 I_r f}{2\pi} \frac{z}{r ((a_i + r)^2 + z^2)^{1/2}} \times \left[ -K(\kappa_i) + \frac{a_i^2 + r^2 + z^2}{(a_i - r)^2 + z^2} E(\kappa_i) \right]$$

where  $K(\kappa_i)$  and  $E(\kappa_i)$  are the complete elliptic integrals of the first and second kinds respectively

- The parameter  $\kappa_i$  is defined by

$$\kappa_i^2 \equiv \frac{4a_i r}{z^2 + (a_i + r)^2}$$

## Electromagnetic modeling

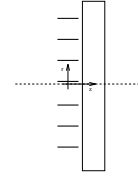


- The vector potential for each of the  $N$  turns of the coil,  $A_{\theta i}(r, z)$ , is given as

$$A_{\theta i}(r, z) = \frac{\mu_0 I_r f}{\pi \kappa_i} \left( \frac{a_i}{r} \right)^{1/2} \times \left[ \left( 1 - \frac{1}{2} \kappa_i^2 \right) K(\kappa_i) - E(\kappa_i) \right]$$

- Here  $a_i$ ,  $i = 0, 1, \dots, N - 1$  are the mean radii of each of the  $N$  turns of the inductive coil and  $r$  is the radial position as measured from the axis of the system

## Electromagnetic modeling



- The axial distance  $d$  from the plane of the coil to the plasma is given by

$$d = \frac{\xi_1}{2} + w_g + w_q + \zeta$$

where

- $\xi_1$  is the width of the copper strip that forms the primary coil
- $w_g$  is the gap size between the near edge of the primary coil and the quartz window
- $w_q$  is the quartz window thickness
- $\zeta$  is the distance from the quartz/plasma boundary into the plasma

## Electromagnetic modeling

- We will normally take  $\zeta = \delta/2$ , where  $\delta$  is the skin depth in the plasma
- Assuming cylindrical symmetry, we have

$$E_\theta(r, z) = -\frac{1}{r} \int_0^r r' \dot{B}_z(r', z) dr'$$

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## Electromagnetic modeling

- The mutual inductance is found by integrating the flux from the inductive coil linking the plasma current in the discharge over all radii

$$M = \frac{2\pi}{I_{rf} I_{\theta o}} \int_0^\infty r B_z(r, d) I_\theta(r) dr$$

- The self inductance

$$L_2 = \frac{2\pi}{I_{\theta o}^2} \int_0^\infty A_\theta(r', z) K_\theta(r', z) r' dr'$$

- $R_2$  and  $L_e$  are determined by the electrical properties of the plasma which are described by the plasma conductivity

$$\sigma_p = \frac{e^2 n_e / m}{\nu_{\text{eff}} + j\omega_{\text{eff}}}$$

where  $\nu_{\text{eff}}$  is the effective collision frequency,  $n_e$  is the electron density and  $\omega_{\text{eff}}$  is the effective driving frequency

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## Electromagnetic modeling

- Because the skin depth  $\delta$  is small compared to typical axial and radial scale lengths, we can write the plasma current density

$$J_\theta(r, z) \approx K_\theta(r) / \delta$$

where  $K_\theta(r)$  is modeled as the surface current density on a perfectly conducting plane located at  $z = d$

$$K_\theta(r) = \frac{2B_r(r)}{\mu_o}$$

- The azimuthal plasma current flowing outside a radius  $r$  is then expressed as

$$I_\theta(r) = \int_r^\infty K_\theta(r') dr'$$

and the total azimuthal plasma current is then  $I_{\theta o} = I_\theta(0)$  where

$$I_{\theta o} = I_{rf} \left( N - \sum_{i=0}^{N-1} \frac{d}{(a_i^2 + d^2)^{1/2}} \right)$$

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## Electromagnetic modeling

- The current profile is assumed to be related to the electric field by Ohm's law  $J_\theta = (\sigma_p + j\omega\epsilon_o)E_\theta$  where the electric field is assumed to follow

$$E_\theta(r, z) \propto E_{\theta o} \exp(-z\gamma)$$

- In our regime, the displacement current is much less than the conduction current and

$$P_{\text{abs}} = 2\pi \int_0^\infty dz \int_0^R r dr \text{Re}[\sigma_p] |E_\theta(r, z)|^2$$

- The rms current flowing through the current path is found by integrating the current density over the cross section of this current path or

$$I_\theta = \int_0^\infty dz \int_0^R dr \sigma_p E_\theta(r, z)$$

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## Electromagnetic modeling

- The resistance of the plasma is then given using  $P_{abs} = R_2 |I_\theta|^2$  as

$$R_2 = \frac{P_{abs}}{|I_\theta|^2} = \frac{\pi |\gamma|^2 \operatorname{Re}[\sigma_p]}{\operatorname{Re}[\gamma] |\sigma_p|^2} \frac{\int_0^R r dr |A_\theta^2(r)|}{\left| \int_0^R dr A_\theta(r) \right|^2}$$

- The electron inertia inductance is found from

$$L_e = \frac{R_2}{\nu_{eff}} \frac{\omega_{eff}}{\omega}$$

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## Electromagnetic modeling

- There is a high voltage across the inductive coil
- Between the coil and the plasma is a dielectric window which acts as a capacitor
- Next to the window a sheath is expected to form with per unit area capacitance  $\sim \epsilon_o/s_m$  where  $s_m$  is the sheath thickness
- In addition there is both ohmic dissipation within the plasma and stochastic dissipation in the plasma sheath

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## Electromagnetic modeling

- Seen in the primary circuit assuming a purely inductive operation, the change in plasma resistance is given by

$$\rho = \frac{\omega^2 M^2 R_2}{R_2^2 + (\omega L_e + \omega L_2)^2}$$

- The change in plasma reactance by

$$\chi = -\frac{\omega^2 M^2 (\omega L_2 + \omega L_e)}{R_2^2 + (\omega L_e + \omega L_2)^2}$$

- The equivalent impedance of the primary coil and the plasma as seen in the primary circuit is

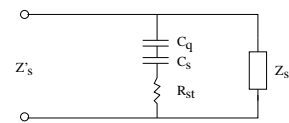
$$Z_s = R_o + \rho + j\omega(L_o - \chi)$$

where  $R_o$  is the resistance and  $L_o$  is the inductance of the primary coil

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## Electromagnetic modeling

- The capacitive terms appear in parallel with the impedance of the coil and the plasma  $Z_s$



- The effective impedance seen in the primary circuit when the plasma is lit becomes

$$Z'_s = \frac{Z_s Z_{cap}}{Z_s + Z_{cap}}$$

where

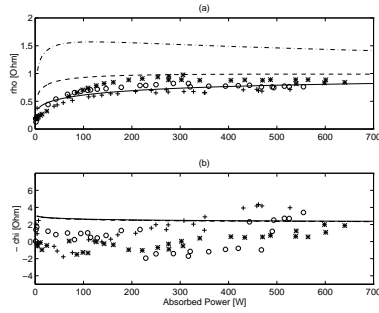
$$Z_{cap} = R_{st} + \frac{1}{j\omega C_s} + \frac{1}{j\omega C_q}$$

where

- $R_{st}$  is the stochastic heating resistance
- $C_s$  is the sheath capacitance
- $C_q$  is the quartz window capacitance

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## Electromagnetic modeling



[Gudmundsson and Lieberman, 1998]

- The changes in primary resistance due to capacitive coupling and plasma loading,  $\rho_{\text{eff}}$
- The negative of the change in primary reactance due to capacitive coupling and plasma loading  $-\chi_{\text{eff}}$ ,
- Argon plasma at — 2 mTorr, - - 10 mTorr and - · - 60 mTorr, compared to measured values for argon plasma

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## Plasma chemistry

- The plasma is either partially or fully ionized gas that contains electrons, ions, neutral atoms and molecules
- The electrons are not in thermal equilibrium with ions and molecules in partially ionized plasma

The plasma chemistry can be complicated

Argon discharge consist of

e, Ar,  $\text{Ar}^+$ ,  $\text{Ar}^*$ , ...

Oxygen discharge consist of

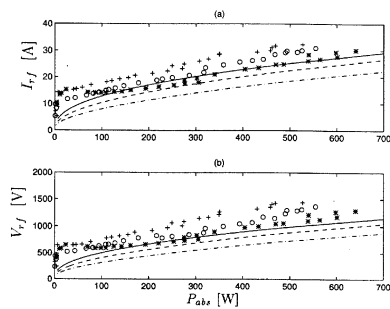
e, O,  $\text{O}_2$ ,  $\text{O}_2^+$ ,  $\text{O}^+$ ,  $\text{O}_2^-$ ,  $\text{O}^-$ ,  $\text{O}_2^*$ ,  $\text{O}^*$ , .....

$\text{SF}_6$  discharge consist of

e,  $\text{SF}_6$ ,  $\text{SF}_5^+$ ,  $\text{SF}_4^+$ ,  $\text{SF}_3^+$ ,  $\text{F}^+$ ,  $\text{F}^-$ ,  $\text{F}^*$ ,  $\text{F}_2$ ,  $\text{F}$ , ...

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## Electromagnetic modeling



[Gudmundsson and Lieberman, 1998]

- The rms rf current  $I_{rf}$  applied to the primary coil versus the power absorbed within the plasma
- The rms rf voltage  $V_{rf}$  applied to the primary coil versus the power absorbed within the plasma
- Argon plasma at — 2 mTorr, - - 10 mTorr and - · - 60 mTorr

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## Global model

The global model is based on:

- Power equilibrium
- Particle conservation for all particles

For argon plasma (noble gas):

Power balance

- Absorbed power = Power loss
- $P_{\text{abs}} = en_0 u_B A_{\text{eff}} \mathcal{E}_T$

Particle balance

- Particle loss at surface = Ionization in bulk
- $n_0 u_B A_{\text{eff}} = k_{iz} n_g n_0 \pi R^2 L$

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## Global model

### Energy loss

The total energy loss for each ion that is lost is

$$\mathcal{E}_T = \mathcal{E}_c + \mathcal{E}_e + \mathcal{E}_i$$

where

- $\mathcal{E}_c$  is the collisional energy loss per electron-ion pair created

$$\mathcal{E}_c = \mathcal{E}_{iz} + \sum_i \mathcal{E}_{ex,i} \frac{k_{ex,i}}{k_{iz}} + \frac{k_{el}}{k_{iz}} \frac{3m_e}{m_i} T_e$$

- $\mathcal{E}_e$  is the average energy of each electron that is lost. If we assume the electron energy to be Maxwellian  $\mathcal{E}_e = 2T_e$
- $\mathcal{E}_i$  is the average kinetic energy of ions that are lost and is determined by the sheath potential

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## Global model

### Advantages

- Give estimate of the plasma parameter with relatively simple calculations ( $n_e, T_e, V_{pl}, n_i$ )
- Tool to estimate which reactions are of importance in particular mixtures

### Limiting factors

- Does not give spatial distribution
- The electron energy distribution is given

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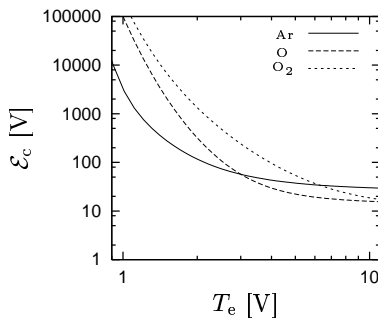
## Global model

### Rate coefficients

- Rate coefficients are calculated from cross sections assuming Maxwellian electron energy distribution

$$k = \left( \frac{2e}{m_e} \right)^{1/2} \int_0^\infty \mathcal{E}^{1/2} \sigma(\mathcal{E}) f(\mathcal{E}) d\mathcal{E}$$

### Collisional energy loss



- The collisional energy loss per electron-ion pair created  $\mathcal{E}_c$

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## Oxygen discharge

- Oxygen is relatively simple diatomic molecule
- The oxygen discharge is weakly electronegative, (negative ions  $O^-$ ,  $O_2^-$  and  $O_3^-$ )
- Negative ions have a significant influence on the discharge due to recombination in the bulk

For electronegative molecular discharge:

- Particle balance
- Quasi neutrality

$$n_e + \sum_i n_{-,i} = \sum_j n_{+,j}$$

- Power balance

$$\frac{P_{abs}}{V} = e \sum_i^{N_0} \mathcal{E}_c^{(X)} k_{iz} n_X n_e + e \sum_i^{N_+} k_{loss}(\mathcal{E}_{e,i} + \mathcal{E}_{i,i}) n_{X+,j}$$

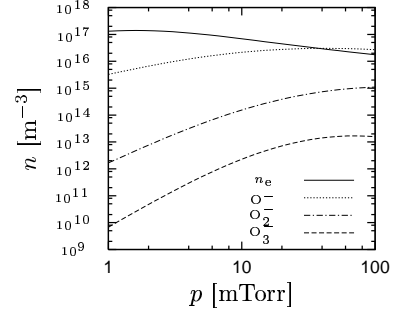
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**Table 1.** The reaction set for oxygen. The rate coefficients for electron-impact collisions were calculated assuming Maxwellian electron energy distribution and fixed over an electron temperature range  $1-20$  eV.

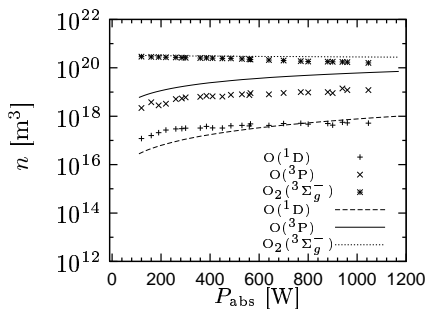
Reaction	Rate coefficient	Reference
$e + O_2 \rightarrow O_2^+ + 2e$	$k_1 = 9 \times 10^{-16} T_e^{-1/2} \exp(-12.4/T_e) \text{ m}^3 \text{ s}^{-1}$	[28]
$e + O_2 \rightarrow O(^1P) + O(^3P)$	$k_2 = 3.2 \times 10^{-16} \text{ m}^3 \text{ s}^{-1}$	[13]
$e + O_2 \rightarrow O(^1P) + O(^1D)$	$k_3 = 1.4 \times 10^{-16} \exp(-4.4/T_e) \text{ m}^3 \text{ s}^{-1}$	[46]
$e + O(^3P) \rightarrow O(^1D) + 2e$	$k_4 = 9.8 \times 10^{-16} T_e^{-1/2} \exp(-3.6/T_e) \text{ m}^3 \text{ s}^{-1}$	[46]
$O(^3P) + O_2 \rightarrow O(^1P) + O_2$	$k_5 = 1.5 \times 10^{-16} 300/T_e \text{ m}^3 \text{ s}^{-1}$	[28]
$O(^3P) + O(^3P) \rightarrow O(^1P) + O(^3P)$	$k_6 = 2.7 \times 10^{-16} 300/T_e \text{ m}^3 \text{ s}^{-1}$	[13]
$e + O(^3P) \rightarrow O(^1P) + 2e$	$k_7 = 1.3 \times 10^{-16} \exp(-3.58/T_e) \text{ m}^3 \text{ s}^{-1}$	[47]
$e + O_2 \rightarrow O(^1P) + O(^3P) + e$	$k_8 = 7.3 \times 10^{-16} \exp(-1.4/T_e) \text{ m}^3 \text{ s}^{-1}$	[13]
$O(^1P) + O(^3P) \rightarrow O_2 + e$	$k_9 = 3.8 \times 10^{-16} 300/T_e \text{ m}^3 \text{ s}^{-1}$	[46]
$e + O_2 \rightarrow O(^3P) + O(^3P) + e$	$k_{10} = 7.3 \times 10^{-17} T_e^{1/2} \exp(-17/T_e) \text{ m}^3 \text{ s}^{-1}$	[46]
$e + O_2 \rightarrow O(^1P) + O(^3P) + e$	$k_{11} = 5.3 \times 10^{-17} T_e^{1/2} \exp(-20/T_e) \text{ m}^3 \text{ s}^{-1}$	[46]
$O(^1D) + O_2 \rightarrow O(^3P) + O_2$	$k_{12} = 2 \times 10^{-16} 300/T_e \text{ m}^3 \text{ s}^{-1}$	[13]
$e + O_2 \rightarrow O(^1P) + O(^3P) + e$	$k_{13} = 1.8 \times 10^{-15} \exp(-11.35/T_e) \text{ m}^3 \text{ s}^{-1}$	[13]
$e + O(^1D) \rightarrow O(^3P) + e$	$k_{14} = 4.5 \times 10^{-15} \exp(-2.39/T_e) \text{ m}^3 \text{ s}^{-1}$	[28]
$O(^1D) + O_2 \rightarrow O(^3P) + O_2$	$k_{15} = 3.8 \times 10^{-15} \text{ m}^3 \text{ s}^{-1}$	[13]
$O(^1D) + O(^3P) \rightarrow 2O(^3P)$	$k_{16} = 1.3 \times 10^{-16} \text{ m}^3 \text{ s}^{-1}$	[28]
$e + O(^1D) \rightarrow O(^3P) + e$	$k_{17} = 9 \times 10^{-16} T_e^{1/2} \exp(-1.4/T_e) \text{ m}^3 \text{ s}^{-1}$	[28]
$e + O_2 \rightarrow O_2(^1\Delta_g) + e$	$k_{18} = 1.7 \times 10^{-15} \exp(-7.1/T_e) \text{ m}^3 \text{ s}^{-1}$	[46]
$e + O_2(^1\Delta_g) \rightarrow O_2(^3\Sigma_g^-) + 2e$	$k_{19} = 9.8 \times 10^{-17} T_e^{-1/2} \exp(-1.2/T_e) \text{ m}^3 \text{ s}^{-1}$	[46]
$e + O_2(^1\Delta_g) \rightarrow O(^3P) + O$	$k_{20} = 2.28 \times 10^{-16} \exp(-2.29/T_e) \text{ m}^3 \text{ s}^{-1}$	[30]
$e + O_2(^1\Delta_g) \rightarrow O_2 + e$	$k_{21} = 5.8 \times 10^{-16} \exp(-2.2/T_e) \text{ m}^3 \text{ s}^{-1}$	[46]
$e + O_2(^1\Delta_g) \rightarrow 2O + e$	$k_{22} = 4.2 \times 10^{-16} \exp(-4.6/T_e) \text{ m}^3 \text{ s}^{-1}$	[46]
$O(^3P) + O_2(^1\Delta_g) \rightarrow O(^3P) + O(^1P)$	$k_{23} = 1.3 \times 10^{-15} 300/T_e \text{ m}^3 \text{ s}^{-1}$	[43]
$O(^3P) + O_2 \rightarrow O_2$	$k_{24} = 2.8 \times 10^{-15} 300/T_e \text{ m}^3 \text{ s}^{-1}$	[46]
$O(^3P) + O(^3P) \rightarrow O_2 + O(^3P)$	$k_{25} = 2.8 \times 10^{-15} 300/T_e \text{ m}^3 \text{ s}^{-1}$	[46]
$e + O_2 + O_2 \rightarrow O(^3P) + O_2 + e$	$k_{26} = 2.26 \times 10^{-15} 300/T_e \text{ m}^3 \text{ s}^{-1}$	[43]
$O(^3P) + O(^3P) + O(^3P) \rightarrow O_2 + O(^3P)$	$k_{27} = 4.9 \times 10^{-16} 300/T_e \text{ m}^3 \text{ s}^{-1}$	[48]
$O(^3P) + O_2(^1\Delta_g) \rightarrow 2O_2 + e$	$k_{28} = 2.7 \times 10^{-15} 300/T_e \text{ m}^3 \text{ s}^{-1}$	[43]
$O(^3P) + O(^3P) \rightarrow O(^3P) + O_2$	$k_{29} = 3.31 \times 10^{-15} 300/T_e \text{ m}^3 \text{ s}^{-1}$	[13]
$e + O_2 \rightarrow O(^3P) + O_2 + e$	$k_{30} = 9.3 \times 10^{-17} T_e^{1/2} \exp(-1.2/T_e) \text{ m}^3 \text{ s}^{-1}$	[45]
$e + O_2 \rightarrow O_2 + e$	$k_{31} = 2.8 \times 10^{-16} \text{ m}^3 \text{ s}^{-1}$	[45]
$O(^3P) + O_2 \rightarrow O_2 + e$	$k_{32} = 5.8 \times 10^{-16} 300/T_e \text{ m}^3 \text{ s}^{-1}$	[13]
$O(^3P) + O_2(^1\Delta_g) \rightarrow O_2 + e$	$k_{33} = 2.2 \times 10^{-15} 300/T_e \text{ m}^3 \text{ s}^{-1}$	[43]
$O(^3P) + O_2 \rightarrow O_2 + e$	$k_{34} = 1.8 \times 10^{-15} 300/T_e \text{ m}^3 \text{ s}^{-1}$	[46]
$O_2 + O_2 \rightarrow 2O_2$	$k_{35} = 2.8 \times 10^{-16} 300/T_e \text{ m}^3 \text{ s}^{-1}$	[46]
$O(^3P) + O_2 \rightarrow O_2 + O$	$k_{36} = 5.3 \times 10^{-16} 300/T_e \text{ m}^3 \text{ s}^{-1}$	[13]
$O(^3P) + O(^3P) \rightarrow O(^3P) + O_2$	$k_{37} = 3.2 \times 10^{-16} 300/T_e \text{ m}^3 \text{ s}^{-1}$	[13]
$O(^3P) + O(^3P) \rightarrow 2O_2 + e$	$k_{38} = 3.8 \times 10^{-16} 300/T_e \text{ m}^3 \text{ s}^{-1}$	[13]
$O(^3P) + O_2 \rightarrow O_2 + O_2$	$k_{39} = 2 \times 10^{-16} 300/T_e \text{ m}^3 \text{ s}^{-1}$	[13]
$O(^3P) + O_2 \rightarrow 2O_2 + e$	$k_{40} = 1.03 \times 10^{-15} 300/T_e \text{ m}^3 \text{ s}^{-1}$	[13]
$O(^3P) + O_2 \rightarrow O_2 + O_2$	$k_{41} = 4 \times 10^{-16} 300/T_e \text{ m}^3 \text{ s}^{-1}$	[13]
$O(^3P) + O(^3P) \rightarrow O_2 + e$	$k_{42} = 3.03 \times 10^{-16} 300/T_e \text{ m}^3 \text{ s}^{-1}$	[13]
$e + O_2 \rightarrow O(^3P) + O_2 + e$	$k_{43} = 1 \times 10^{-16} 300/T_e \text{ m}^3 \text{ s}^{-1}$	[13]
$2O_2 + O(^3P) \rightarrow O_2 + O_2$	$k_{44} = 6.9 \times 10^{-16} 300/T_e \text{ m}^3 \text{ s}^{-1}$	[13]
$O(^3P) + 2O(^3P) \rightarrow O_2 + O(^3P)$	$k_{45} = 5.12 \times 10^{-16} \text{ m}^3 \text{ s}^{-1}$	[13]
$e + O(^3P) + O_2 \rightarrow O(^3P) + O_2 + e$	$k_{46} = 1 \times 10^{-16} \text{ m}^3 \text{ s}^{-1}$	[13]
$e + O(^3P) + O_2 \rightarrow O(^3P) + O_2 + e$	$k_{47} = 1 \times 10^{-16} \text{ m}^3 \text{ s}^{-1}$	[13]
$e + O_2 \rightarrow O(^3P) + O(^3P) + e$	$k_{48} = 2.11 \times 10^{-15} 300/T_e \text{ m}^3 \text{ s}^{-1}$	[13]
$O_2 + O(^3P) \rightarrow O_2 + O(^3P) + O(^3P)$	$k_{49} = 1.8 \times 10^{-15} 300/T_e \text{ m}^3 \text{ s}^{-1}$	[13]

## Oxygen discharge



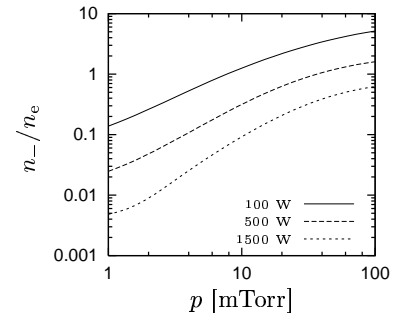
- The densities of electrons  $n_e$  and negative oxygen ions,  $O^-$ ,  $O_2^-$ , and  $O_3^-$ , versus discharge pressure at 500 W and flowrate 50 sccm for a cylindrical stainless steel chamber with  $L = 7.6$  cm and  $R = 15.2$  cm

## Oxygen discharge



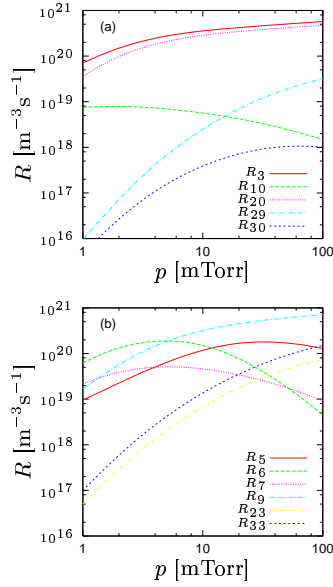
- The neutral densities of atomic and molecular oxygen as well as the lowest excited states versus absorbed power
- The measurements by Fuller et al. [Fuller et al., 2000] was made in an inductively coupled discharge in a cylindrical stainless steel chamber with  $R = 18$  cm and  $L = 22$  cm. The operating pressure was 10 mTorr

## Oxygen discharge



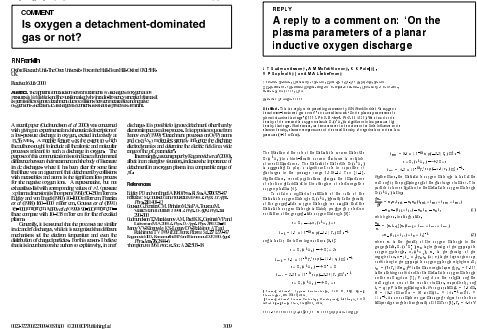
- The electronegativity  $n_e/(n_- + n_2- + n_3-)$  at 100, 500 and 1500 W versus discharge pressure
- We assume flowrate to be 50 sccm and a cylindrical stainless steel chamber with  $L = 7.6$  cm and  $R = 15.2$  cm

## Creation - destruction of $O^-$



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## The metastable $O_2(a^1\Delta_g)$

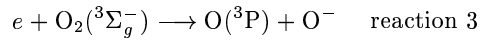


[Franklin, 2000] and  
[Gudmundsson et al., 2000]

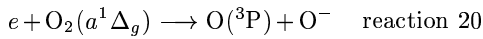
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## Creation - destruction of $O^-$

- Creation of the negative ion  $O^-$  is mainly through

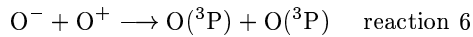


or

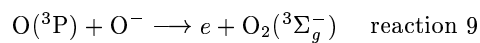


in the pressure range 1 – 100 mTorr

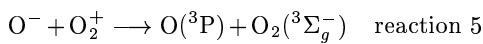
- Destruction is mainly through



at low pressure (< 10 mTorr) and



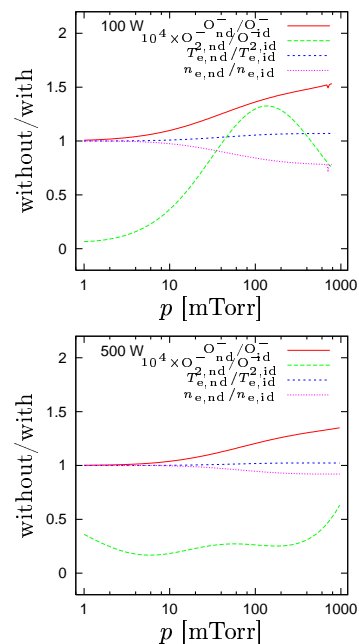
or



at higher pressure 10 – 100 mTorr

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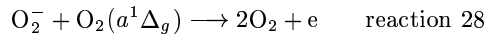
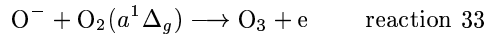
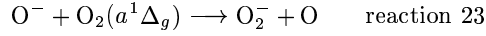
## The metastable $O_2(a^1\Delta_g)$



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## The metastable $O_2(a^1\Delta_g)$

- The model was applied to investigate the influence of the metastable molecule  $O_2(a^1\Delta_g)$  on the discharge
- The influence of neglecting the reactions



on the plasma parameters

- The effects are negligible at low pressure but the error increases with increasing pressure

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## Summary

- The low pressure inductive discharge was introduced
- A first principles electromagnetic model of a planar inductive discharge was described:
  - It was used to calculate the rf voltage and current applied to drive argon discharge
  - It was applied to estimate the current induced in the discharge
- A global model of an oxygen discharge was used to:
  - Investigate creation and destruction of  $O^-$
  - Look at the influence of the metastable molecule  $O_2(a^1\Delta_g)$