

Háskóli Íslands

Verkfræðideild

Rafmagns- og tölvuverkfræðiskor

Vor 2004

## **08.32.23 Smárásir**

### **Formúlublað**

## 1 Fastar

$$q = 1.602 \times 10^{-19} \text{ C}$$

$$N_{\text{Av}} = 6.022 \times 10^{23} \text{ sameindir/mól}$$

$$k = 1.38 \times 10^{-23} \text{ J/K} = 8.62 \times 10^{-5} \text{ eV/K}$$

$$\epsilon_0 = 8.854 \times 10^{-14} \text{ F/cm}$$

$$\epsilon_{\text{ox}}/\epsilon_0 = 3.9$$

$$\epsilon_{\text{Si}}/\epsilon_0 = 11.9$$

$$\epsilon_{\text{Ge}}/\epsilon_0 = 16$$

$$\epsilon_{\text{GaAs}}/\epsilon_0 = 13.1$$

Fyrir kísil við stofuhita:

$$n_i = 9.65 \times 10^9 \text{ cm}^{-3}$$

Fyrir GaAs við stofuhita:

$$n_i = 2.25 \times 10^9 \text{ cm}^{-3}$$

## 2 Ræktun

$$k_0 = \frac{C_s}{C_1}$$

$$C_s = k_0 C_0 \left[ 1 - \frac{M}{M_0} \right]^{k_0 - 1}$$

## 3 Hálfeiðarar

$$E_{\text{H}} = -\frac{m_e q^4}{8\epsilon_0^2 h^2 n^2} = -\frac{13.6}{n^2}$$

$$E_{\text{g}} = 1.17 - \frac{(4.73 \times 10^{-4})T^2}{(T + 636)} \quad \text{kísill}$$

$$E_{\text{g}} = 1.52 - \frac{(5.4 \times 10^{-4})T^2}{(T + 204)} \quad \text{GaAs}$$

$$m^* = \frac{\hbar^2}{d^2 E / dk^2}$$

$$f(E) = \frac{1}{1 + \exp\left(\frac{E - E_{\text{F}}}{kT}\right)}$$

$$n = \int_{\infty}^{E_c} f(E) N(E) dE$$

$$N(E) = 4\pi \left(\frac{2m^*}{h^2}\right)^{3/2} E^{1/2}$$

$$f(E) \approx \exp\left(-\frac{E - E_{\text{F}}}{kT}\right) \text{ ef } E - E_{\text{F}} > 3kT$$

$$f(E) \approx 1 - \exp\left(-\frac{E_{\text{F}} - E}{kT}\right) \text{ ef } E - E_{\text{F}} < 3kT$$

$$n \approx N_c \exp\left(-\frac{E_c - E_{\text{F}}}{kT}\right)$$

$$N_c = 2 \left(\frac{2\pi m^* kT}{h^2}\right)^{3/2}$$

$$p \approx N_v \exp\left(-\frac{E_{\text{F}} - E_v}{kT}\right)$$

$$N_v = 2 \left(\frac{2\pi m^* kT}{h^2}\right)^{3/2}$$

$$np = N_c N_v \exp\left(-\frac{E_g}{kT}\right) = n_i^2$$

$$n = n_i \exp\left(\frac{E_F - E_i}{kT}\right)$$

$$p = n_i \exp\left(\frac{E_i - E_F}{kT}\right)$$

$$E_c - E_F = kT \ln\left(\frac{N_c}{N_D}\right)$$

$$E_F - E_v = kT \ln\left(\frac{N_v}{N_A}\right)$$

$$np = n_i^2$$

Við stofuhita fyrir kísil

$$N_c = 2.8 \times 10^{19} \text{ cm}^{-3}$$

$$N_v = 1.04 \times 10^{19} \text{ cm}^{-3}$$

Við stofuhita fyrir GaAs

$$N_c = 4.7 \times 10^{17} \text{ cm}^{-3}$$

$$N_v = 7 \times 10^{18} \text{ cm}^{-3}$$

n-leiðandi hálfleiðari

$$n_n = \frac{1}{2} \left[ N_D - N_A + \sqrt{(N_D - N_A)^2 + 4n_i^2} \right]$$

og

$$p_n = \frac{n_i^2}{n_n}$$

p-leiðandi hálfleiðari

$$p_p = \frac{1}{2} \left[ N_A - N_D + \sqrt{(N_A - N_D)^2 + 4n_i^2} \right]$$

og

$$n_p = \frac{n_i^2}{p_p}$$

$$N_C = 2 \left( \frac{m_e^* kT}{2\pi\hbar^2} \right)^{3/2}$$

$$N_V = 2 \left( \frac{m_h^* kT}{2\pi\hbar^2} \right)^{3/2}$$

$$J = \sigma \mathcal{E}$$

$$\sigma = \frac{nq^2\tau}{m_n^*} \quad [\Omega\text{cm}]^{-1}$$

$$\sigma = qn\mu_n$$

$$\mu_n = \frac{q\tau}{m_n^*}$$

$$J = q(n\mu_n + p\mu_p)\mathcal{E} = \sigma \mathcal{E}$$

$$R = \frac{\rho L}{Wd} = \frac{L}{Wd\sigma}$$

## 4 MOSFET

MOS kjörtvistur

$$q\phi_{ms} = q(\phi_m - \phi_s)$$

$$q\phi_{ms} = q\phi_m - \left[ q\chi + \frac{E_g}{2} + q\phi_b \right]$$

$$Q_{sc} = -qN_A x_{dmax} \approx -\sqrt{2q\epsilon_s N_A (2\psi_b)}$$

$$\psi_s(\text{umhverfing}) \approx 2\psi_b = \frac{2kT}{q} \ln\left(\frac{N_A}{n_i}\right)$$

## 5 Viðnám

$$x_{\text{dmax}} = \left( \frac{2\epsilon_s \psi_s (\text{umhv.})}{qN_A} \right)^{1/2} \approx \left( \frac{2\epsilon_s (2\psi_b)}{qN_A} \right)^{1/2}$$

$$R = \frac{\rho L}{A}$$

$$C_{\text{ox}} = \frac{\epsilon_{\text{ox}}}{d}$$

$$C_{\text{d}} = \frac{\epsilon_s}{x_{\text{d}}}$$

$$C = \frac{C_{\text{ox}} C_{\text{d}}}{C_{\text{ox}} + C_{\text{d}}}$$

$$\sigma = \frac{1}{\rho} = (q\mu_n n + q\mu_p p)$$

$$R = \frac{1}{G} = \frac{L}{Wg}$$

$$I_{\text{D}} \approx \frac{W}{L} \mu_n C_{\text{ox}} (V_{\text{G}} - V_{\text{T}}) V_{\text{D}}$$

$$\text{ef } V_{\text{D}} \ll (V_{\text{G}} - V_{\text{T}})$$

$$V_{\text{T}} \approx \frac{\sqrt{2\epsilon_s q N_A (2\psi_b)}}{C_{\text{ox}}} + 2\psi_b$$

$$V_{\text{Dsat}} \approx V_{\text{G}} - 2\psi_b + K^2 \left[ 1 - \left( 1 + \frac{2V_{\text{G}}}{K^2} \right)^{1/2} \right]$$

þar sem

$$K \equiv \frac{\epsilon_{\text{Si}} q N_A}{C_{\text{ox}}}$$

$$I_{\text{Dsat}} \approx \frac{W \mu_n C_{\text{ox}}}{2L} (V_{\text{G}} - V_{\text{T}})^2$$

Frávik frá kjörhegðan

$$V_{\text{FB}} = \phi_{\text{ms}} - \frac{Q_{\text{it}}}{C_{\text{ox}}}$$

$$V_{\text{T}} = \phi_{\text{ms}} - \frac{Q_{\text{it}}}{C_{\text{ox}}} - \frac{Q_{\text{sc}}}{C_{\text{ox}}} + 2\psi_b$$

$$\psi_b = (E_{\text{i}} - E_{\text{F}})/q$$

$$\Delta V_{\text{T}} = \frac{\sqrt{2q\epsilon_s N_A}}{C_{\text{o}}} \left[ (2\psi_b + V_{\text{BS}})^{1/2} - (2\psi_b)^{1/2} \right]$$

$$x_{\text{S}} = \left( \frac{2\epsilon_s}{qN_A} (V_{\text{bi}} + V_{\text{BS}}) \right)^{1/2}$$

$$x_{\text{D}} = \left( \frac{2\epsilon_s}{qN_A} (V_{\text{D}} + V_{\text{bi}} + V_{\text{BS}}) \right)^{1/2}$$

## 6 Hreyfifræði gass

$$pV = RT = N_{\text{Av}} kT$$

$$f_v = \frac{4}{\sqrt{\pi}} \left( \frac{m}{2kT} \right)^{3/2} v^2 \exp \left( -\frac{mv^2}{2kT} \right)$$

$$\phi = \frac{p}{(2\pi mkT)^{1/2}} = 3.51 \times 10^{22} \left( \frac{p}{\sqrt{MT}} \right)$$

## 7 Lagvöxtur

$$C_{\text{s}} = \frac{C_{\text{g}}}{1 + (k_{\text{s}}/h_{\text{g}})}$$

$$v = \frac{k_{\text{s}} h_{\text{g}}}{k_{\text{s}} + h_{\text{g}}} \left( \frac{C_{\text{t}}}{C_{\text{a}}} \right) y$$

$$\delta(x) \approx \sqrt{\frac{\mu x}{\rho_{\text{d}} v}}$$

$$\bar{\delta}(x) = \frac{1}{L} \int_0^L \delta(x) dx = \frac{2}{3} \sqrt{\frac{\mu L}{\rho_{\text{d}} v}}$$

$$h_{\text{g}} = \frac{D_{\text{g}}}{\delta} = \frac{3}{2} D_{\text{g}} \sqrt{\frac{v \rho_{\text{d}}}{\mu L}}$$

## 8 Oxun

$$x^2 + \frac{2D}{k}x = \frac{2DC_0}{C_1}(t + \tau)$$

$$\tau \equiv \left( d_0^2 + \frac{2Dd_0}{k} \right) \frac{C_1}{2DC_0}$$

$$x = \frac{D}{k} \left[ \left( 1 + \frac{2C_0k^2(t + \tau)}{DC_1} \right)^{1/2} - 1 \right]$$

$$x^2 + Ax = B(t + \tau)$$

$$A \equiv \frac{2D}{k}$$

$$B \equiv \frac{2DC_0}{C_1}$$

$$\frac{B}{A} \equiv \frac{kC_0}{C_1}$$

## 9 Sveim

$$F = -D \frac{\partial C}{\partial x}$$

$$\frac{\partial C}{\partial t} = -\frac{\partial F}{\partial x} = \frac{\partial}{\partial x} \left( D \frac{\partial C}{\partial x} \right)$$

$$D = D_0 \exp \left( -\frac{E_a}{kT} \right)$$

Fastur yfirborðspéttleiki

$$C(x, t) = C_s \operatorname{erfc} \left( \frac{x}{2\sqrt{Dt}} \right)$$

$$Q(t) = \int_0^\infty C(x, t) dx$$

$$Q(t) = \frac{2}{\sqrt{\pi}} C_s \sqrt{Dt} \approx 1.13 C_s \sqrt{Dt}$$

Föst heildaríbót

$$\int_0^\infty C(x, t) dx = S$$

$$C(\infty, t) = 0$$

$$C(x, t) = \frac{S}{\sqrt{\pi Dt}} \exp \left( -\frac{x^2}{4Dt} \right)$$

$$C_s(t) = \frac{S}{\sqrt{\pi Dt}}$$

## 10 Jónaígræðsla

$$\left( \frac{dE}{dx} \right)_{\text{tot}} = S_n(E) + S_e(E)$$

$$\int_0^R dx = R = - \int_E^0 \frac{dE}{\left( \frac{dE}{dx} \right)_{\text{tot}}}$$

$$S_e = k_e \sqrt{E}$$

$$N(x) = N_p \exp \left[ -\frac{(x - R_p)^2}{2(\Delta R_p)^2} \right]$$

$$Q = \int_0^\infty N(x) dx$$

$$Q = \sqrt{2\pi} N_p \Delta R_p$$

$$N(x) = \frac{N_p}{\left[ 1 + \frac{4Dt}{2(\Delta R_p)^2} \right]^{1/2}} \exp \left[ -\frac{(x - R_p)^2}{2(\Delta R_p)^2 + 4Dt} \right]$$

## 11 Málmar

$$\text{MTF} \sim \frac{1}{J^2} \exp\left(\frac{E_a}{kT}\right)$$

## 12 Lithography

$$\text{CD} = W_{\min} \approx \sqrt{\lambda g}$$

$$R = \frac{0.61\lambda}{n \sin \theta}$$

$$R = \frac{0.61\lambda}{\text{NA}} = k_1 \frac{\lambda}{\text{NA}}$$

$$\text{NA} \equiv n \sin \theta$$

$$\text{DOF} = \pm \frac{R/2}{\tan \theta} \approx \pm \frac{R/2}{\sin \theta} = \pm k_2 \frac{\lambda}{(\text{NA})^2}$$

$$\text{MTF} = \frac{I_{\text{MAX}} - I_{\text{MIN}}}{I_{\text{MAX}} + I_{\text{MIN}}}$$

$$\text{CMTF}_{\text{viðnám}} = \frac{E_T - E_1}{E_T + E_1} = \frac{10^{1/\gamma} - 1}{10^{1/\gamma} + 1}$$

$$\gamma = \frac{1}{\log\left[\frac{E_T}{E_1}\right]}$$

## 13 Framleiðni

Líkan Poisson

$$Y = \frac{1}{e^{AD}}$$

Líkan Murphy

$$Y = \left[ \frac{1 - e^{-AD}}{AD} \right]^2$$

Líkan Seeds

$$Y = \frac{1}{e^{\sqrt{AD}}}$$