Kjarna- og öreindafræði

Dæmablað 1

Skilafrestur 14. September 2016 kl. 15:00

1. Neutron – proton capture (10)

A neutron and a proton can undergo radioactive capture at rest

 $\mathbf{p} + \mathbf{n} \longrightarrow \mathbf{d} + \gamma$

Find the energy of the photon emitted in this capture. Is the recoil of the deuteron important ?

2. A gold foil (10)

A gold foil 0.02 cm thick is irradiated by a beam of thermal neutrons with a flux of 10^{12} neutrons/cm²/s. The nuclide ¹⁹⁸Au with a half-life of 2.7 days is produced by the reaction ¹⁹⁷Au(n, γ)¹⁹⁸Au. The density of gold is 19.3 g/cm³ and the cross section for the above reaction is 97.8 ×10⁻²⁴ cm². ¹⁹⁷Au is 100 % naturally abundant.

(a) If the foil is irradiated for 5 minutes, what is the 198 Au activity of the foil in decays/cm²/s?

(b) What is the maximum amount of $^{198}\mathrm{Au/cm^2}$ that can be produced in the foil?

(c) How long must the foil be irradiated if it is to have 2/3 of its maximum activity?

3. Decay chain (20)

A parent isotope has a half-life $T_{1/2} = 10^4 \text{ yr} = 3.15 \times 10^{11} \text{ s}$. It decays through a series of radioactive daughters to a final stable isotope. Among the daughters the

greatest half-life is 20 yr. Others are less than a year. At t = 0 one has 10^{20} parent nuclei but no daughters.

(a) At t = 0 what is the activity (decays/sec) of the parent isotope ?

(b) How long does it take for the population of the 20 yr isotope to reach approximately 97 % of its equilibrium value ?

(c) At t = 104 yr how many nuclei of the 20 yr isotope are present? Assume that none of the decays leading to the 20 yr isotope is branched.

(d) The 20 yr isotope has two competing decay modes: α , 99.5 %; β , 0.5 %. At t = 104 yr, what is the activity of the isotope which results from the β -decay ?

(e) Among the radioactive daughters, could any reach their equilibrium populations much more quickly (or much more slowly) than the 20 yr isotope ?